Hoise School A-Level Mathematics Information Booklet

Well done for choosing one of the most popular A-level courses and I hope you are excited to continue your journey through Mathematics this September!

This booklet contains some important information that you will need <u>before</u> you start the course, so please read it carefully.

If you have any questions, please do get in touch by email.

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n <u>r.green@holt.wokingham.sch.uk</u>

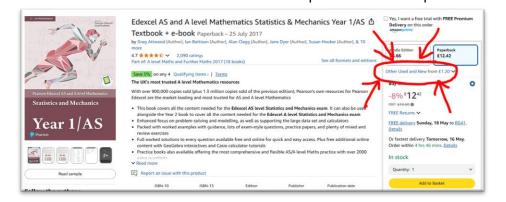
Required Equipment

Textbooks:

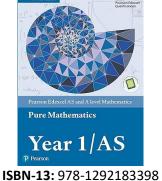
We are following the *Pearson Edexcel* A-Level Maths course.

You will need the Pure book from the first lesson in September.

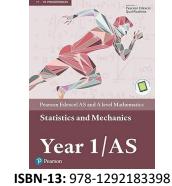
New textbooks usually include a digital copy too, but second hand is fine. You may be able to find a Year 13 student wanting to sell these on. I recommend checking the **"Other used and New"** tab on Amazon for some cheap second-hand copies.



Pearson Edexcel AS and A level Mathematics Pure Mathematics Year 1/AS



Pearson Edexcel AS and A level Mathematics Statistics & Mechanics Year 1/AS



Calculator:

You will need an A-level appropriate calculator.

We very strongly recommend you purchase a Casio graphical calculator.

The vast majority of students and staff use a **Casio fx-CG50** graphical calculator and we will teach you how to use it during the course. Any Casio graphical calculator is fine, but the more similar it is to your classmates/teacher, the easier you will find it to learn.

Note: From September 2025, Casio are no longer selling the fx-CG50 and are replacing it with the newer fx-CG100 model. You may find the fx-CG50 hard to find in stock from September.

Look on eBay for second-hand calculators, although a new one is a good investment. I think <u>www.studentcalculators.co.uk</u> have reasonably priced new calculators compared to high-street shops.









Casio fx-9860G-III

Essential Bridging Tasks

A level Maths builds on the GCSE and we will assume that you have a sound grasp of these skills from the very start of the course.

We also know that maths can go rusty very quickly if you do not practice it.

With that in mind it is essential that you do some practice over the summer in order to get off to the best start possible on the A level course.

You will have an induction test in the first few weeks of your maths course to check your understanding and see if more support is needed. Completing the bridging work will help prepare you for this.

Main Bridging Task: AMSP Transition to A-level Maths Course

- We would like you to sign up to and complete as much of the AMSP's "Transition to A-level Mathematics" course as possible. This uses the Integral maths website which we also use throughout Y12 and Y13.
- The course is an interactive series of online videos, presentations, and questions that cover the essential topics for A-level success such as:
 - Integers & proof Algebraic Manipulation
 - Geometry

- Trigonometry
- Surds & Indices
- Completing the Square
- Coordinate Geometry
- At the end of the course you can download a certificate which we would like you to share with your teacher in September.
- Please sign-up for the free course here: <u>Register for Course</u> Alternatively, email <u>r.green@holt.wokingham.sch.uk</u> to be signed up.
- More info available here: Transition to A level Mathematics course AMSP

Transition t	o A level Mat	homotics			
Dashboard / I	My courses / Transiti	on Alevel			
Welcon	ne				
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Alternative Bridging Task: Practice Tasks

If you choose not to complete the Transition to A-Level Maths course above, then I strongly recommend you at least check your skills by completing the practice tasks at the end of this booklet instead.

These cover:

- Expanding Brackets
- Surds
- Indices
- Factorising

Complete these tasks and mark your work. Make sure you do corrections.

Optional Bridging Task: Essential Skills

Transition to A level Mathematics resources: Essential Skills | AMSP

The above website has some excellent resources to refresh and stretch your GCSE knowledge. You may want to use it in conjunction with the above tasks as there are some help videos and explanations you may find useful.

There are 6 sections:

- Simplifying
- Expanding
- Factorising
- Rearranging
- Solving
- Sketching

The tasks range from routine practice through to some more challenging problems to solve. Please use the website to help recap, practice and inspire you. Have fun with the problems!

Optional Bridging Task: Learn Your Graphical Calculator

Your calculator is only useful to you if you know how to use it. We will guide you through it in lessons, but you may want to have a look at some of these guides and activities.

Resources Archive - Casio Calculators

Scroll down the page and look at how to do various Calculations, Equations and Functions. Ignore the sections that you don't recognise, e.g. matrices and finance section.

Enrichment

Maths is a rich and varied subject that spans across cultures and throughout human history. Wider reading and engagement in the mathematical world outside of your studies will not only enrich your understanding and enjoyment of the course but can be a lot of fun.

Here are some resources that members of The Holt School Maths Department recommend.



Hidden Figures (Film)	More or Less: Behind the Statistics (Radio Show/Podcast)	Gresham College Maths Lectures (Talks)	
The set of	B B C MORE OR LESS 4	GRESHAM COLLEGE SINCE 1597	
The story of a team of female African-American mathematicians who served a vital role in NASA during the early years of the U.S. space program.	A weekly radio show and podcast, hosted by economist Tim Harford examining the truth behind numbers and claims made by politicians and newspapers. Available on BBC Sounds: <u>BBC Sounds - More or Less:</u> <u>Behind the Stats</u>	Accessible and interesting lectures on popular maths topic from some of the world's leadin mathematicians, scientists and authors. Such as "How to Prove = 0" and "The Maths of Boomerangs" Available here: Browse All Gresham Colleg	
Sumaze! App/Game	The Science Museum (London) <i>Trip</i>	Numberphile Youtube	
	SCIENCE MUSEUM	JL	
Download the free sumaze! apps. No instructions, learn by playing. Once you have completed the logarithms levels, research logarithms online. Can you find the unknown values below?	From war and peace to life, death, money, trade and beauty, the objects in Mathematics: The Winton Gallery reveal how mathematics connects to every aspect of our lives. <u>Mathematics: The Winton</u> <u>Gallery Science Museum</u>	"Video's about numbers and stuff" – A huge collection of short videos hosted by top mathematicians, scientists ar maths popularisers to discus strange and wonderful applications of maths. <u>Numberphile - YouTube</u>	

What follows are the <u>Practice Tasks</u> for the alternative bridging work task. (Answers are at the end)

Expanding brackets and simplifying expressions

A LEVEL LINKS

Scheme of work: 1a. Algebraic expressions - basic algebraic manipulation, indices and surds

Key points

- When you expand one set of brackets you must multiply everything inside the bracket by what is outside.
- When you expand two linear expressions, each with two terms of the form ax + b, where $a \neq 0$ and $b \neq 0$, you create four terms. Two of these can usually be simplified by collecting like terms.

Examples

Example 1 Expand 4(3x-2)

4(3x - 2) = 12x - 8	Multiply everything inside the bracket by the 4 outside the bracket
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Example 2 Expand and simplify 3(x+5) - 4(2x+3)

3(x+5) - 4(2x+3) = 3x + 15 - 8x - 12	1 Expand each set of brackets separately by multiplying $(x + 5)$ by 3 and $(2x + 3)$ by -4
= 3 - 5x	2 Simplify by collecting like terms: 3x - 8x = -5x and $15 - 12 = 3$

Example 3 Expand and simplify (x + 3)(x + 2)

(x+3)(x+2) = x(x+2) + 3(x+2)	1 Expand the brackets by multiplying $(x + 2)$ by x and $(x + 2)$ by 3
$= x^{2} + 2x + 3x + 6$	2 Simplify by collecting like terms:
= x ² + 5x + 6	2x + 3x = 5x

Example 4 Expand and simplify (x - 5)(2x + 3)

(x-5)(2x+3) = x(2x+3) - 5(2x+3)	1 Expand the brackets by multiplying $(2x + 3)$ by x and $(2x + 3)$ by -5
$= 2x^{2} + 3x - 10x - 15$ $= 2x^{2} - 7x - 15$	2 Simplify by collecting like terms: 3x - 10x = -7x

Practice

1	Expand. a $3(2x-1)$ c $-(3xy-2y^2)$	b	$-2(5pq + 4q^2)$	Watch out
2	Expand and simplify. a $7(3x+5) + 6(2x-8)$ c $9(3s+1) - 5(6s-10)$		8(5p-2) - 3(4p+9) 2(4x-3) - (3x+5)	dividing) positive negative number the signs are the the answer is '+' signs are differe
3	Expand. a $3x(4x + 8)$ c $-2h(6h^2 + 11h - 5)$		$4k(5k^2 - 12) -3s(4s^2 - 7s + 2)$	
4	Expand and simplify. a $3(y^2 - 8) - 4(y^2 - 5)$ c $4p(2p - 1) - 3p(5p - 2)$		2x(x+5) + 3x(x-7) $3b(4b-3) - b(6b-9)$	
5	Expand $\frac{1}{2}(2y-8)$			
6	Expand and simplify. a $13 - 2(m+7)$	b	$5p(p^2+6p)-9p(2p-3)$	
7	The diagram shows a rectangle. Write down an expression, in terms of the rectangle. Show that the area of the rectangle can $21x^2 - 35x$		3x - 5	7x
8	Expand and simplify. a $(x + 4)(x + 5)$ c $(x + 7)(x - 2)$ e $(2x + 3)(x - 1)$ g $(5x - 3)(2x - 5)$ i $(3x + 4y)(5y + 6x)$ k $(2x - 7)^2$	d f h	(x + 7)(x + 3) (x + 5)(x - 5) (3x - 2)(2x + 1) (3x - 2)(7 + 4x) (x + 5) ² (4x - 3y) ²	
	· ·		· · · ·	

Extend

- Expand and simplify $(x + 3)^2 + (x 4)^2$ 9
- **10** Expand and simplify.
 - **a** $\left(x+\frac{1}{x}\right)\left(x-\frac{2}{x}\right)$ **b** $\left(x+\frac{1}{x}\right)^2$

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Surds and rationalising the denominator

A LEVEL LINKS

Scheme of work: 1a. Algebraic expressions - basic algebraic manipulation, indices and surds

Key points

- A surd is the square root of a number that is not a square number, for example $\sqrt{2}$, $\sqrt{3}$, $\sqrt{5}$, etc.
- Surds can be used to give the exact value for an answer.

•
$$\sqrt{ab} = \sqrt{a} \times \sqrt{b}$$

•
$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

- To rationalise the denominator means to remove the surd from the denominator of a fraction.
- To rationalise $\frac{a}{\sqrt{b}}$ you multiply the numerator and denominator by the surd \sqrt{b}
- To rationalise $\frac{a}{b+\sqrt{c}}$ you multiply the numerator and denominator by $b-\sqrt{c}$

Examples

Example 1 Simplify $\sqrt{50}$

$\sqrt{50} = \sqrt{25 \times 2}$	1 Choose two numbers that are factors of 50. One of the factors must be a square number
$=\sqrt{25}\times\sqrt{2}$	2 Use the rule $\sqrt{ab} = \sqrt{a} \times \sqrt{b}$
$=5 \times \sqrt{2}$	3 Use $\sqrt{25} = 5$
$=5\sqrt{2}$	

Example 2 Simplify $\sqrt{147} - 2\sqrt{12}$

$\sqrt{147} - 2\sqrt{12}$ $= \sqrt{49 \times 3} - 2\sqrt{4 \times 3}$	1 Simplify $\sqrt{147}$ and $2\sqrt{12}$. Choose two numbers that are factors of 147 and two numbers that are factors of 12. One of each pair of factors must be a square number
$=\sqrt{49}\times\sqrt{3}-2\sqrt{4}\times\sqrt{3}$	2 Use the rule $\sqrt{ab} = \sqrt{a} \times \sqrt{b}$
$=7\times\sqrt{3}-2\times2\times\sqrt{3}$	3 Use $\sqrt{49} = 7$ and $\sqrt{4} = 2$
$=7\sqrt{3}-4\sqrt{3}$ $=3\sqrt{3}$	4 Collect like terms

Example 3 Simplify $(\sqrt{7} + \sqrt{2})(\sqrt{7} - \sqrt{2})$

$$(\sqrt{7} + \sqrt{2})(\sqrt{7} - \sqrt{2})$$

$$= \sqrt{49} - \sqrt{7}\sqrt{2} + \sqrt{2}\sqrt{7} - \sqrt{4}$$

$$= 7 - 2$$

$$= 5$$

$$1 \quad \text{Expand the brackets. A common mistake here is to write } (\sqrt{7})^2 = 49$$

$$2 \quad \text{Collect like terms:}$$

$$-\sqrt{7}\sqrt{2} + \sqrt{2}\sqrt{7}$$

$$= -\sqrt{7}\sqrt{2} + \sqrt{7}\sqrt{2} = 0$$

Example 4 Rationalise
$$\frac{1}{\sqrt{3}}$$

$\frac{1}{\sqrt{3}} = \frac{1}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$	1 Multiply the numerator and denominator by $\sqrt{3}$
$=\frac{1\times\sqrt{3}}{\sqrt{9}}$	2 Use $\sqrt{9} = 3$
$=\frac{\sqrt{3}}{3}$	

Example 5	Rationalise and simplify	$\frac{\sqrt{2}}{\sqrt{12}}$
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$$\frac{\sqrt{2}}{\sqrt{12}} = \frac{\sqrt{2}}{\sqrt{12}} \times \frac{\sqrt{12}}{\sqrt{12}}$$

$$= \frac{\sqrt{2} \times \sqrt{4 \times 3}}{12}$$

$$= \frac{\sqrt{2} \times \sqrt{4 \times 3}}{12}$$

$$= \frac{\sqrt{2} \times \sqrt{4 \times 3}}{12}$$

$$= \frac{\sqrt{2} \sqrt{2} \sqrt{3}}{12}$$

$$= \frac{\sqrt{2} \sqrt{2}}{12}$$

$$= \frac{\sqrt{2} \sqrt{3}}{6}$$
1 Multiply the numerator and denominator by $\sqrt{12}$
2 Simplify $\sqrt{12}$ in the numerator. Choose two numbers that are factors of 12. One of the factors must be a square number
3 Use the rule $\sqrt{ab} = \sqrt{a} \times \sqrt{b}$
4 Use $\sqrt{4} = 2$
5 Simplify the fraction:

$$\frac{2}{12}$$
 simplifies to $\frac{1}{6}$

Example 6	Rationalise and simplify $\frac{3}{2+\sqrt{5}}$		
	$\frac{3}{2+\sqrt{5}} = \frac{3}{2+\sqrt{5}} \times \frac{2-\sqrt{5}}{2-\sqrt{5}}$	1	Multiply the numerator and denominator by $2 - \sqrt{5}$
	$=\frac{3\left(2-\sqrt{5}\right)}{\left(2+\sqrt{5}\right)\left(2-\sqrt{5}\right)}$	2	Expand the brackets
	$=\frac{6-3\sqrt{5}}{4+2\sqrt{5}-2\sqrt{5}-5}$	3	Simplify the fraction
	$= \frac{6-3\sqrt{5}}{-1}$ $= 3\sqrt{5}-6$	4	Divide the numerator by -1 Remember to change the sign of all terms when dividing by -1

Practice

3

1	Sim	plify.			Hint
	a	$\sqrt{45}$	b	$\sqrt{125}$	One of the two
	c	$\sqrt{48}$	d	$\sqrt{175}$	numbers you
	e	$\sqrt{300}$	f	$\sqrt{28}$	choose at the start must be a square
	g	<u>√72</u>	h	$\sqrt{162}$	number.

2	Sim	plify.			Watch out!
	a	$\sqrt{72} + \sqrt{162}$	b	$\sqrt{45} - 2\sqrt{5}$	Check you have
	c	$\sqrt{50} - \sqrt{8}$	d	$\sqrt{75} - \sqrt{48}$	chosen the
	e	$2\sqrt{28} + \sqrt{28}$	f	$2\sqrt{12} - \sqrt{12} + \sqrt{27}$	highest square number at the

Ex	pand and simplify.		
a	$(\sqrt{2}+\sqrt{3})(\sqrt{2}-\sqrt{3})$	b	$(3+\sqrt{3})(5-\sqrt{12})$
c	$(4-\sqrt{5})(\sqrt{45}+2)$	d	$(5+\sqrt{2})(6-\sqrt{8})$

4 Rationalise and simplify, if possible.

a
$$\frac{1}{\sqrt{5}}$$
b $\frac{1}{\sqrt{11}}$ c $\frac{2}{\sqrt{7}}$ d $\frac{2}{\sqrt{8}}$ e $\frac{2}{\sqrt{2}}$ f $\frac{5}{\sqrt{5}}$ g $\frac{\sqrt{8}}{\sqrt{24}}$ h $\frac{\sqrt{5}}{\sqrt{45}}$

5 Rationalise and simplify. **a** $\frac{1}{3-\sqrt{5}}$ **b** $\frac{2}{4+\sqrt{3}}$ **c** $\frac{6}{5-\sqrt{2}}$

Extend

- 6 Expand and simplify $(\sqrt{x} + \sqrt{y})(\sqrt{x} \sqrt{y})$
- 7 Rationalise and simplify, if possible.

a
$$\frac{1}{\sqrt{9}-\sqrt{8}}$$
 b $\frac{1}{\sqrt{x}-\sqrt{y}}$

Rules of indices

A LEVEL LINKS

Scheme of work: 1a. Algebraic expressions – basic algebraic manipulation, indices and surds

Key points

• $a^m \times a^n = a^{m+n}$

•
$$\frac{a^m}{a^n} = a^{m-n}$$

- $(a^m)^n = a^{mn}$
- $a^0 = 1$
- $a^{\frac{1}{n}} = \sqrt[n]{a}$ i.e. the *n*th root of *a*

•
$$a^{\frac{m}{n}} = \sqrt[n]{a^m} = \left(\sqrt[n]{a}\right)^m$$

•
$$a^{-m} = \frac{1}{a^m}$$

• The square root of a number produces two solutions, e.g. $\sqrt{16} = \pm 4$.

Examples

Example 1 Evaluate 10⁰

$10^0 = 1$	Any value raised to the power of zero is equal to 1
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Example 2 Evaluate $9^{\frac{1}{2}}$

Evaluate $27^{\frac{2}{3}}$

Example 3

 $27^{\frac{2}{3}} = \left(\sqrt[3]{27}\right)^2$ $= 3^2$ = 9 **1** Use the rule $a^{\frac{m}{n}} = \left(\sqrt[n]{a}\right)^m$ **2** Use $\sqrt[3]{27} = 3$

Example 4 Evaluate 4^{-2}

$4^{-2} = \frac{1}{4^2}$	1 Use the rule $a^{-m} = \frac{1}{a^m}$
$=\frac{1}{16}$	2 Use $4^2 = 16$

Example 5 Simplify $\frac{6x^5}{2x^2}$

$$\frac{6x^5}{2x^2} = 3x^3$$

$$6 \div 2 = 3 \text{ and use the rule } \frac{a^m}{a^n} = a^{m-n} \text{ to}$$
give $\frac{x^5}{x^2} = x^{5-2} = x^3$

Simplify $\frac{x^3 \times x^5}{x^4}$

$\frac{x^3 \times x^5}{x^4} = \frac{x^{3+5}}{x^4} = \frac{x^8}{x^4}$	1 Use the rule $a^m \times a^n = a^{m+n}$
$= x^{8-4} = x^4$	2 Use the rule $\frac{a^m}{a^n} = a^{m-n}$

Example 7

Write $\frac{1}{3x}$ as a single power of x

$\frac{1}{3x} = \frac{1}{3}x^{-1}$	Use the rule $\frac{1}{a^m} = a^{-m}$, note that the
	fraction $\frac{1}{3}$ remains unchanged

Example 8

Write $\frac{4}{\sqrt{x}}$ as a single power of x

$\frac{4}{\sqrt{x}} = \frac{4}{x^{\frac{1}{2}}}$	1 Use the rule $a^{\frac{1}{n}} = \sqrt[n]{a}$
$=4x^{-\frac{1}{2}}$	2 Use the rule $\frac{1}{a^m} = a^{-m}$

Practice

1	Evaluate. a 14 ⁰	b	3 ⁰	c	5 ⁰	d	<i>x</i> ⁰
2	Evaluate. a $49^{\frac{1}{2}}$	b	$64^{\frac{1}{3}}$	с	$125^{\frac{1}{3}}$	d	$16^{\frac{1}{4}}$
3	Evaluate. a $25^{\frac{3}{2}}$	b	$8^{\frac{5}{3}}$	С	$49^{\frac{3}{2}}$	d	$16^{\frac{3}{4}}$
4	Evaluate. a 5^{-2}	b	4 ⁻³	с	2-5	d	6 ⁻²

Simplify.

a	$\frac{3x^2 \times x^3}{2x^2}$	b	$\frac{10x^5}{2x^2 \times x}$
c	$\frac{3x \times 2x^3}{2x^3}$	d	$\frac{7x^3y^2}{14x^5y}$
e	$\frac{y^2}{y^{\frac{1}{2}} \times y}$	f	$\frac{c^{\frac{1}{2}}}{c^2 \times c^{\frac{3}{2}}}$
g	$\frac{\left(2x^2\right)^3}{4x^0}$	h	$\frac{x^{\frac{1}{2}} \times x^{\frac{3}{2}}}{x^{-2} \times x^3}$

Watch out!	
Remember that	
any value raised to	
the power of zero	
is 1. This is the	
rule <i>a</i> ⁰ = 1.	

Evaluate.

a
$$4^{-\frac{1}{2}}$$
 b $27^{-\frac{2}{3}}$ **c** $9^{-\frac{1}{2}} \times 2^{3}$
d $16^{\frac{1}{4}} \times 2^{-3}$ **e** $\left(\frac{9}{16}\right)^{-\frac{1}{2}}$ **f** $\left(\frac{27}{64}\right)^{-\frac{2}{3}}$

7 Write the following as a single power of x.
a
$$\frac{1}{x}$$
 b $\frac{1}{x^7}$ c $\sqrt[4]{x}$
d $\sqrt[5]{x^2}$ e $\frac{1}{\sqrt[3]{x}}$ f $\frac{1}{\sqrt[3]{x^2}}$

- 8 Write the following without negative or fractional powers.
 - **a** x^{-3} **b** x^{0} **c** $x^{\frac{1}{5}}$ **d** $x^{\frac{2}{5}}$ **e** $x^{-\frac{1}{2}}$ **f** $x^{-\frac{3}{4}}$
- 9 Write the following in the form ax^n .
 - **a** $5\sqrt{x}$ **b** $\frac{2}{x^3}$ **c** $\frac{1}{3x^4}$ **d** $\frac{2}{\sqrt{x}}$ **e** $\frac{4}{\sqrt[3]{x}}$ **f** 3

Extend

10 Write as sums of powers of *x*.

a
$$\frac{x^5 + 1}{x^2}$$
 b $x^2 \left(x + \frac{1}{x} \right)$ **c** $x^{-4} \left(x^2 + \frac{1}{x^3} \right)$

Factorising expressions

A LEVEL LINKS

Scheme of work: 1b. Quadratic functions – factorising, solving, graphs and the discriminants

Key points

- Factorising an expression is the opposite of expanding the brackets.
- A quadratic expression is in the form $ax^2 + bx + c$, where $a \neq 0$.
- To factorise a quadratic equation find two numbers whose sum is b and whose product is ac.
- An expression in the form $x^2 y^2$ is called the difference of two squares. It factorises to (x y)(x + y).

Examples

Example 1 Factorise $15x^2y^3 + 9x^4y$

$15x^2y^3 + 9x^4y = 3x^2y(5y^2 + 3x^2)$	The highest common factor is $3x^2y$. So take $3x^2y$ outside the brackets and then divide each term by $3x^2y$ to find the terms in the brackets
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Example 2 Factorise $4x^2 - 25y^2$

$4x^2 - 25y^2 = (2x + 5y)(2x - 5y)$	This is the difference of two squares as the two terms can be written as $(2x)^2$ and $(5y)^2$
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Example 3 Factorise $x^2 + 3x - 10$

b = 3, ac = -10	1 Work out the two factors of $ac = -10$ which add to give $b = 3$
So $x^2 + 3x - 10 = x^2 + 5x - 2x - 10$	 (5 and -2) 2 Rewrite the <i>b</i> term (3<i>x</i>) using these two factors
= x(x+5) - 2(x+5)	3 Factorise the first two terms and the last two terms
= (x+5)(x-2)	4 $(x+5)$ is a factor of both terms

Example 4 Factorise $6x^2 - 11x - 10$

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b = -11, ac = -60	1 Work out the two factors of $ac = -60$ which add to give $b = -11$
So	(-15 and 4)
$6x^2 - 11x - 10 = 6x^2 - 15x + 4x - 10$	2 Rewrite the <i>b</i> term $(-11x)$ using
	these two factors
= 3x(2x-5) + 2(2x-5)	3 Factorise the first two terms and the
	last two terms
=(2x-5)(3x+2)	4 $(2x-5)$ is a factor of both terms

Example 5	Simplify $\frac{x^2 - 4x - 21}{2x^2 + 9x + 9}$	
	$\frac{x^2 - 4x - 21}{2x^2 + 9x + 9}$	1 Factorise the numerator and the denominator
	For the numerator: b = -4, $ac = -21So$	2 Work out the two factors of $ac = -21$ which add to give $b = -4$ (-7 and 3)
	$x^2 - 4x - 21 = x^2 - 7x + 3x - 21$	3 Rewrite the <i>b</i> term $(-4x)$ using these two factors
	=x(x-7)+3(x-7)	4 Factorise the first two terms and the last two terms
	= (x-7)(x+3)	5 $(x-7)$ is a factor of both terms
	For the denominator: b = 9, ac = 18 So	6 Work out the two factors of ac = 18 which add to give $b = 9(6 and 3)$
	$2x^2 + 9x + 9 = 2x^2 + 6x + 3x + 9$	7 Rewrite the <i>b</i> term $(9x)$ using these two factors
	= 2x(x+3) + 3(x+3)	8 Factorise the first two terms and the last two terms
	=(x+3)(2x+3)	9 $(x+3)$ is a factor of both terms
	$\frac{x^2 - 4x - 21}{2x^2 + 9x + 9} = \frac{(x - 7)(x + 3)}{(x + 3)(2x + 3)}$ $= \frac{x - 7}{2x + 3}$	10 $(x + 3)$ is a factor of both the numerator and denominator so cancels out as a value divided by itself is 1
	-	numerator and denominator so cancels out as a value divided by

Practice

1	Fac	ctorise.		
	a	$6x^4y^3 - 10x^3y^4$	b	$21a^3b^5 + 35a^5b^2$
	c	$25x^2y^2 - 10x^3y^2 + 15x^2y^3$		
2	Fac	ctorise		
	a	$x^2 + 7x + 12$	b	$x^2 + 5x - 14$
	c	$x^2 - 11x + 30$	d	$x^2 - 5x - 24$
	e	$x^2 - 7x - 18$	f	$x^2 + x - 20$
	g	$x^2 - 3x - 40$	h	$x^2 + 3x - 28$

3 Factorise

a	$36x^2 - 49y^2$	b	$4x^2 - 81y^2$
с	$18a^2 - 200b^2c^2$		

4 Factorise

a	$2x^2 + x - 3$	b	$6x^2 + 17x + 5$
c	$2x^2 + 7x + 3$	d	$9x^2 - 15x + 4$
e	$10x^2 + 21x + 9$	f	$12x^2 - 38x + 20$

5 Simplify the algebraic fractions.

a	$\frac{2x^2 + 4x}{x^2 - x}$	b	$\frac{x^2+3x}{x^2+2x-3}$
c	$\frac{x^2-2x-8}{x^2-4x}$	d	$\frac{x^2 - 5x}{x^2 - 25}$
e	$\frac{x^2 - x - 12}{x^2 - 4x}$	f	$\frac{2x^2 + 14x}{2x^2 + 4x - 70}$

6 Simplify

a
$$\frac{9x^2 - 16}{3x^2 + 17x - 28}$$

b $\frac{2x^2 - 7x - 15}{3x^2 - 17x + 10}$
c $\frac{4 - 25x^2}{10x^2 - 11x - 6}$
d $\frac{6x^2 - x - 1}{2x^2 + 7x - 4}$

Extend

7 Simplify
$$\sqrt{x^2 + 10x + 25}$$

8 Simplify $\frac{(x+2)^2 + 3(x+2)^2}{x^2 - 4}$

Hint

Take the highest common factor outside the bracket.

Answers Expanding Brackets

1	a	6 <i>x</i> – 3	b	$-10pq - 8q^2$
	c	$-3xy + 2y^2$		
2	a	21x + 35 + 12x - 48 = 33x - 13		
	b	40p - 16 - 12p - 27 = 28p - 43		
	с	27s + 9 - 30s + 50 = -3s + 59 = 59	9 – 3	S
	d	8x - 6 - 3x - 5 = 5x - 11		
3		$12x^2 + 24x$		$20k^3 - 48k$
	c	$10h - 12h^3 - 22h^2$	d	$21s^2 - 21s^3 - 6s$
4		-2 1	Ŀ	$5x^2 - 11x$
4		$-y^2 - 4$ $2p - 7p^2$		$\frac{5x^2 - 11x}{6b^2}$
	c	$2p - 1p^{2}$	a	0 <i>D</i> 2
5	у —	4		
	5			
6	a	-1 - 2m	b	$5p^3 + 12p^2 + 27p$
7	7 <i>x</i> ($3x - 5) = 21x^2 - 35x$		
8		$x^2 + 9x + 20$		$x^2 + 10x + 21$
		$x^2 + 5x - 14$		$x^2 - 25$
		$2x^2 + x - 3$		$6x^2 - x - 2$
		$10x^2 - 31x + 15$		$12x^2 + 13x - 14$
		$18x^2 + 39xy + 20y^2$	•	$x^2 + 10x + 25$
	k	$4x^2 - 28x + 49$	1	$16x^2 - 24xy + 9y^2$
	- 2			
9	$2x^2$	-2x+25		

10 a
$$x^2 - 1 - \frac{2}{x^2}$$
 b $x^2 + 2 + \frac{1}{x^2}$

Answers Surds

1	a	3√5	b	5√5
		4√3		5√7
	e	$10\sqrt{3}$	f	2√7
	g	6√2	h	9√2
		-		_
2		15√2		√5
		3√2	d	$\sqrt{3}$
	e	6√7	f	5√3
2		1	,	0 5
3		-1	D	$9-\sqrt{3}$
	c	10√5−7	d	$26 - 4\sqrt{2}$
		$\sqrt{5}$		$\sqrt{11}$
4		$\frac{\sqrt{5}}{5}$		$\frac{\sqrt{11}}{11}$
4				
4	c	$\frac{2\sqrt{7}}{7}$	d	$\frac{\sqrt{2}}{2}$
4	c	$\frac{2\sqrt{7}}{7}$	d f	$\frac{\sqrt{2}}{2}$ $\sqrt{5}$
4	c	$\frac{2\sqrt{7}}{7}$	d f	$\frac{\sqrt{2}}{2}$ $\sqrt{5}$
4	c		d f	$\frac{\sqrt{2}}{2}$
	c e g	$\frac{2\sqrt{7}}{7}$	d f h	$\frac{\sqrt{2}}{2}$ $\sqrt{5}$

 $\mathbf{c} \qquad \frac{6(5+\sqrt{2})}{23}$

7 a
$$3+2\sqrt{2}$$
 b $\frac{\sqrt{x}+\sqrt{y}}{x-y}$

Answers Indices

1	a	1	b	1	c	1	d	1
2	a	7	b	4	c	5	d	2
3	a	125	b	32	c	343	d	8
4	a	$\frac{1}{25}$	b	$\frac{1}{64}$	c	$\frac{1}{32}$	d	$\frac{1}{36}$
5	a	$\frac{3x^3}{2}$	b	$5x^2$				
	c	3 <i>x</i>	d	$\frac{y}{2x^2}$				
		$\frac{y^{\frac{1}{2}}}{2x^6}$	f h	c ⁻³ x				
6		$\frac{1}{2}$		$\frac{1}{9}$	c			
	d	$\frac{1}{4}$	e	$\frac{4}{3}$	f	$\frac{16}{9}$		
7	a			x ⁻⁷		$x^{\frac{1}{4}}$		
	d	$x^{\frac{2}{5}}$	e	$x^{-\frac{1}{3}}$	f	$x^{-\frac{2}{3}}$		
8	a	$\frac{1}{x^3}$	b		c	$\sqrt[5]{x}$		
	d	$\sqrt[5]{x^2}$	e	$\frac{1}{\sqrt{x}}$	f	$\frac{1}{\sqrt[4]{x^3}}$		
		$5x^{\frac{1}{2}}$		2 <i>x</i> ⁻³	c	$\frac{1}{3}x^{-4}$		
	d	$2x^{-\frac{1}{2}}$	e	$4x^{-\frac{1}{3}}$	f	$3x^{0}$		
10	a	$x^3 + x^{-2}$	b	$x^3 + x$	c	$x^{-2} + x^{-7}$		

Answers factorising

a c	$2x^{3}y^{3}(3x - 5y) 5x^{2}y^{2}(5 - 2x + 3y)$	b	$7a^3b^2(3b^3+5a^2)$
c e	(x-5)(x-6) (x-9)(x+2)	d f	(x + 7)(x - 2) (x - 8)(x + 3) (x + 5)(x - 4) (x + 7)(x - 4)
a c	(6x - 7y)(6x + 7y) 2(3a - 10bc)(3a + 10bc)	b	(2x-9y)(2x+9y)
c	(2x+1)(x+3)	d	(3x + 1)(2x + 5) (3x - 1)(3x - 4) 2(3x - 2)(2x - 5)
a	$\frac{2(x+2)}{x-1}$	b	$\frac{x}{x-1}$
c	$\frac{x+2}{x}$	d	$\frac{x}{x+5}$
e	$\frac{x+3}{x}$	f	$\frac{x}{x-5}$
a	$\frac{3x+4}{x+7}$	b	$\frac{2x+3}{3x-2}$
c	$\frac{2-5x}{2x-3}$	d	$\frac{3x+1}{x+4}$
	c a c a c a c e a c e a	a $(x+3)(x+4)$ c $(x-5)(x-6)$ e $(x-9)(x+2)$ g $(x-8)(x+5)$ a $(6x-7y)(6x+7y)$ c $2(3a-10bc)(3a+10bc)$ a $(x-1)(2x+3)$ c $(2x+1)(x+3)$ e $(5x+3)(2x+3)$ a $\frac{2(x+2)}{x-1}$ c $\frac{x+2}{x}$ e $\frac{x+3}{x}$ a $\frac{3x+4}{x+7}$	c $5x^2y^2(5-2x+3y)$ a $(x+3)(x+4)$ b c $(x-5)(x-6)$ d e $(x-9)(x+2)$ f g $(x-8)(x+5)$ h a $(6x-7y)(6x+7y)$ b c $2(3a-10bc)(3a+10bc)$ a $(x-1)(2x+3)$ b c $(2x+1)(x+3)$ d e $(5x+3)(2x+3)$ f a $\frac{2(x+2)}{x-1}$ b c $\frac{x+2}{x}$ d e $\frac{x+3}{x}$ f a $\frac{3x+4}{x+7}$ b

7
$$(x+5)$$

 $8 \qquad \frac{4(x+2)}{x-2}$